

# MODULE 4: POLYNOMIALS

*"WE ARE ALL SELF MADE, BUT ONLY THE SUCCESSFUL ADMIT IT."*

## 4.4 POLYNOMIALS

Polynomial Type

Example

Monomial: \_\_\_\_\_

Binomial: \_\_\_\_\_

Trinomial: \_\_\_\_\_

Polynomial: \_\_\_\_\_

Terms are separated by \_\_\_\_\_ and \_\_\_\_\_.

Polynomial Degree: determined by the highest \_\_\_\_\_.

Leading Coefficient: coefficient with highest \_\_\_\_\_.

Given the polynomial:  $a^6 + 9a^5 - 2a^{10} - 8a^3 + 3$

List the terms: \_\_\_\_\_

List the coefficients of each term \_\_\_\_\_

Find the degree of each term: \_\_\_\_\_

Find the degree of the polynomial: \_\_\_\_\_

Find the leading coefficient: \_\_\_\_\_

Evaluate: \_\_\_\_\_ and \_\_\_\_\_.

Always plug in with \_\_\_\_\_.

Ex. Evaluate  $-2xy - x^3$  when  $x = -3$  and  $y = -2$

#### 4.5 ADDING AND SUBTRACTING POLYNOMIALS

Always \_\_\_\_\_ anything in front of the parentheses first.

Drop the parentheses if it is a \_\_\_\_\_. No change occurs.

If it is a \_\_\_\_\_, then distribute the negative sign and change the signs of each term within the parentheses.

When combining like terms, remember like terms have the same \_\_\_\_\_ and the same \_\_\_\_\_.

Note: Use symbols to organize like terms into separate groups.

Ex. Simplify:  $5x^2 - 3x + 4x^2 - 7x + 6$

Ex. Simplify:  $(x^2 - 5x - 7) + (3x^2 + 4x - 5)$

Ex. Simplify:  $(-4x + 6) - (2x^2 - 6x^2 - 3)$

Ex. Simplify:  $(9x^2 - x + 5) - (4x^2 + 3x - 6)$

#### 4.6 MULTIPLYING POLYNOMIALS

Multiplying polynomials: Use the \_\_\_\_\_ property.

Ex. Simplify:  $-3x^2(-x^4 + 3x^2 - 1)$

Ex. Simplify:  $-5x^3y(3x^2y^4 - 7x^2 + 4y^3 - 2)$

If multiplying 2 *expressions* (side by side) use the acronym: FOIL

F \_\_\_\_\_

O \_\_\_\_\_

I \_\_\_\_\_

L \_\_\_\_\_

Ex. Simplify:  $(3x + 2)(5x - 9)$

Ex. Simplify:  $(x - 5)(-3x - 8)$

Ex. Simplify:  $(x - 7)(x + 9)$

Multiplication is \_\_\_\_\_. (order doesn't matter)

Ex. Simplify:  $2x(3x + 5)(x - 3)$

Ex. Simplify:  $-x(8x + 6)(7x - 9)$

If multiplying a perfect square, write the expression \_\_\_\_\_.

Note: Do not ever distribute the exponent into an expression!

Ex. Simplify:  $(3x)^2$

Note: This a monomial squared (no +/-)

Ex. Simplify:  $(3x - 7)^2$

Note: This a binomial squared (expression with +/-); must FOIL

Ex. Simplify:  $(x + 4)^2$

Ex. Simplify:  $(2x + \frac{1}{4})^2$

\_\_\_\_\_ Pairs: Expressions that look to be the same (same terms), but with opposite signs in the middle.

Ex. Simplify:  $(5x - 6)(5x + 6)$

Note: When you FOIL conjugate pairs, the 2 middle terms cancel

If multiplying conjugate pairs you can skip the outer and inner portion of F.O.I.L., only multiply the first and the last terms.

Ex. Simplify:  $(9x - 8)(9x + 8)$

Ex. Simplify:  $(x^2 - 7)(x^2 + 7)$

#### **4.7 DIVISION OF POLYNOMIALS**

Note: Properties of exponents for division tells me to

\_\_\_\_\_ exponents.

Ex. Simplify:  $\frac{30x^4y^3}{15x^2y^7}$

Ex. Simplify:  $\frac{6x^5y^2z^2}{54x^5yz^{10}}$

When dividing with an expression on the top, and a monomial on the bottom, first \_\_\_\_\_ your fraction, then use properties of exponents for division

Ex. 
$$\frac{10x^2 - 8x + 4}{2}$$

Ex. 
$$\frac{90x^3 - 72x^2 + 54x}{-9x}$$

Ex. 
$$\frac{20x^3y^3 - 75x^4y^5 + 35x^6y^8}{5x^2y^3}$$

Ex. 
$$\frac{6a^{12}b^7 - 3a^7b^{10} + 15a^5b^3}{3a^5b^3}$$

#### Homework Checklist

- Section 4.4 Polynomials*
- Section 4.5 Polynomials: Adding and Subtracting*
- Section 4.6 & 4.7 Polynomials: Multiplying/Dividing*